

$B(X, Y) = \{ f : f \text{ is a bounded function with } f: X \rightarrow Y \}$

e.g. If  $X = [0, 10]$ ,  $Y = \mathbb{R}$

$f: [0, 10] \rightarrow \mathbb{R}$  with  $f(x) = x$

Then  $f \in B([0, 10], \mathbb{R})$ .

If  $g: [0, 10] \rightarrow \mathbb{R}$  with

$$g(x) = \begin{cases} 0 & \text{if } x = 0 \\ \frac{1}{x} & \text{if } x > 0, \end{cases}$$

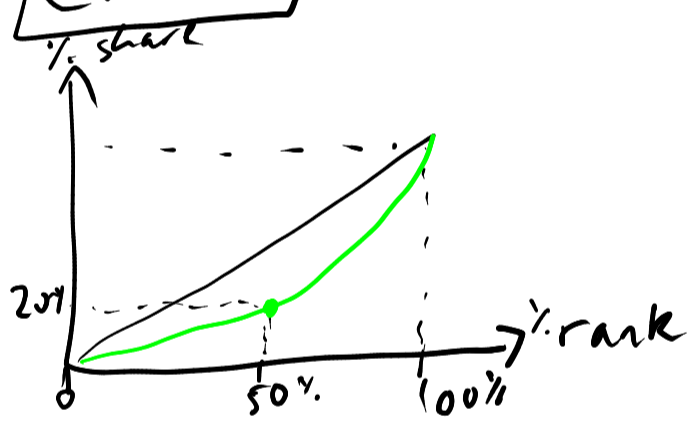
then  $g \notin B([0, 10], \mathbb{R})$ , because  $g$  is unbounded.

If  $h: \mathbb{R} \rightarrow \mathbb{R}$  and  $h(x) = 0$

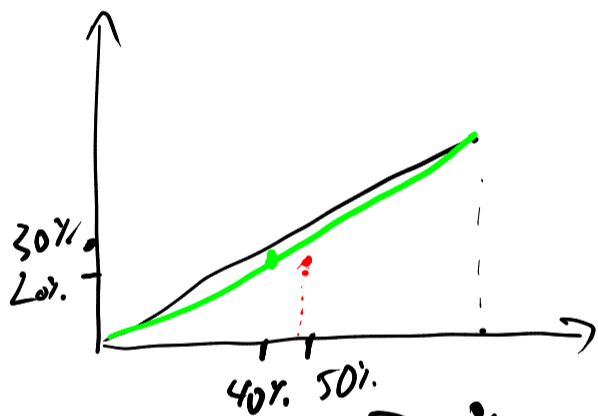
then  $h \notin B([0, 10], \mathbb{R})$  because it has the wrong domain.

Note: it's implied here that  $d_1 = d_2$ , but this need not be.

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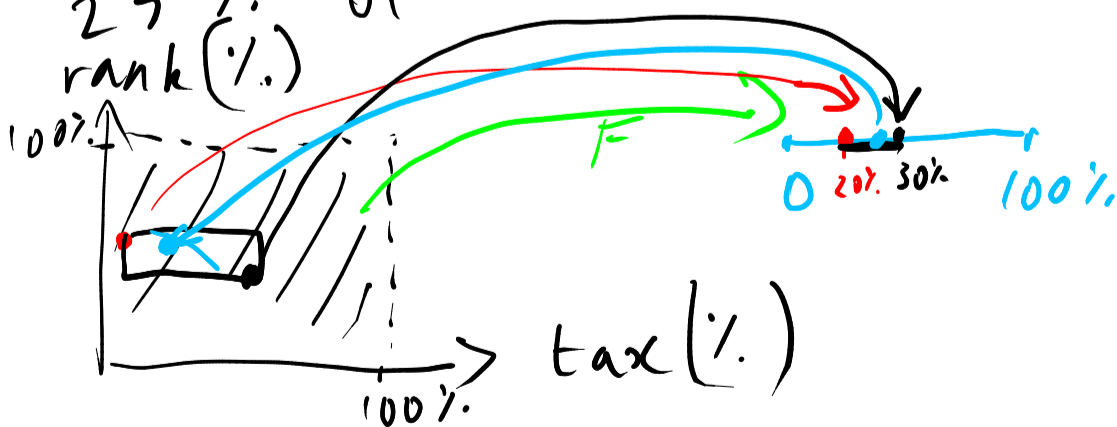


tax = 1%  
 $F(0.5, 0.01) = 0.2$   
s rank tax %share



tax = 50%  
 $F(0.4, 0.5) = 0.3$

Prove there is some tax between 1% & 50%, and some rank between 40% - 50% s.t. they earn 25% of the income



Lipschitz

