

Churchill wins: $\{(Atlee, 0), (Churchill, 10^6)\}$
all of the votes

Churchill wins by one vote

$\{(Atlee, 499999), (Churchill, 500001)\}$

^{set of} All possible outcomes:

$\{(Atlee, n), (Churchill, 10^6 - n)\}$
s.t. $n \in \mathbb{N}$ and $0 \leq n \leq 10^6$

B13 (i) Negate: for all $x > 0$, $\sqrt{x} > 0$.

Answer: there exist some $x > 0$ such that $\sqrt{x} \leq 0$.

Axiomatic approach:

de Morgan laws:

for all $x > 0$, $\sqrt{x} > 0$
is the same thing as
it is false that
there exists some $x > 0$
such that it is false that
 $\sqrt{x} > 0$.

Or he might have written

$\forall x > 0, \sqrt{x} > 0$

is the same as

$\neg \exists x > 0, \neg \sqrt{x} > 0$

it never happens that something went wrong

Therefore, the negation of these statements is

$\neg \neg \exists x > 0, \neg \sqrt{x} > 0$

double negation cancels out

which is the same as

$\exists x > 0, \neg \sqrt{x} > 0$

and $\exists x > 0, \sqrt{x} \leq 0$.

(iii) Negate: All punishments fit the crime.

Reformulate: For all crimes c , the punishment for that crime $p(c)$ fits the crime c .

Negation: there exists a crime c such that the punishment $p(c)$ does not fit the crime c .

Axiomatic/formal approach:

reformulate:

$\forall c, p(c)$ fits c .

$\Leftrightarrow \neg \exists c, \neg p(c)$ fits c

negation: $\neg \neg \exists c, \neg p(c)$ fits c

$\Leftrightarrow \exists c, \neg p(c)$ fits c

From the audience.

I defined a set

$X = \{f : [0,1] \rightarrow [0,1]\}$.

\uparrow X is the set of functions whose domains are $[0,1]$, and whose co-domains are $[0,1]$.

$g(x) = x^2$ where $\text{dom}(g) = [0,1]$
 $\text{co-dom}(g) = [0,1]$

Yes, $g \in X$

$h(x) = x^2$ where $\text{dom}(h) = \mathbb{R}$
 $\text{co-dom}(h) = \mathbb{R}$.

No, $h \notin X$.